# A thermodynamic method based on isoequilibrium behavior to determine the values of stereoelectronic parameters of phosphines 

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#### Abstract

Isoequilibrium behavior provides a method of determining stereoelectronic parameters, for use in linear free energy relationships. This method is based on thermodynamics and is different from the usual ways of assigning values to these parameters. Analysis of isoequilibrium behavior is done in terms of the three parameter QALE (quantitative analysis of ligand effects) model, with parameters $\chi, \theta$ and $E_{\mathrm{ar}}$. We use this method to interpret new $E^{\circ} / T$ values of the $\eta-\mathrm{Cp}(\mathrm{CO})(\mathrm{L}) \mathrm{Fe}(\mathrm{COMe})^{+/ 0}$ couple $\left(\mathrm{Cp}=\right.$ cyclopentadienyl, $\left.\mathrm{L}=\mathrm{PPh}_{i} \mathrm{R}_{3-i}\right)$ and establish a way to calculate $\chi$ and $E_{\text {ar }}$ values for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$. In support of the validity of the method, we find that these calculated $\chi$ values agree well, except for $\mathrm{PPh}_{2} \mathrm{Pr}^{\mathrm{i}}$, with the values previously reported by Bartik. We also calculated a value for $\chi$ equal to 0.4 for $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ for which a $\chi$ value had not been reported previously.


## Introduction

Isoequilibrium behavior ${ }^{1-19}$ for a process involving a set of compounds occurs when a plot of $\Delta G^{\circ} / T$ versus $1 / T$ shows a fan-shaped array of lines with a single point of intersection [equivalently, $\Delta H^{\circ}$ (slope) is linearly related to $\Delta S^{\circ}$ (intercept)]. In principle, at this point, called the isoequilibrium point, the variations of $\Delta G^{\circ}$ become independent of the stereoelectronic properties of the substituents or ligands. The isoequilibrium point simply arises from the linear extrapolation of the experimental data and reflects the linear relationship between $\Delta S^{\circ}$ and $\Delta H^{\circ}$ over an experimental range of temperature where both $\Delta H^{\circ}$ and $\Delta S^{\circ}$ may be treated as constant. This point often occurs outside the experimental range and even occurs at negative temperatures. The observation of isoequilibrium or isokinetic behavior for a set of related compounds is believed to indicate that a system is responding to variations in a single stereoelectronic parameter "although the physical meaning of this parameter might not be known". ${ }^{2}$ In this study, we identify this single parameter and show that in the general case for an $n$ parameter system, this parameter is comprised of a linear combination of a maximum of $n-1$ parameters. We will show in this study that we can use isoequilibrium behavior to determine $\chi$ values (vide infra) for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ in a manner very different from the spectroscopic methods that have been used previously. ${ }^{20}$

We have been working on combining isoequilibrium behavior ${ }^{21,22}$ and the QALE model (quantitative analysis of ligand effects) of phosphorus(III) ligand effects. ${ }^{23-45}$ In the QALE model a physiochemical property is related to the QALE parameters via eqn. (1),

$$
\begin{equation*}
\text { property }=a \chi+b \theta+b^{\prime}\left(\theta-\theta_{\mathrm{st}}\right) \lambda+c E_{\mathrm{ar}}+d \tag{1}
\end{equation*}
$$

where $\chi$ is a measure of the electron donor capacity ${ }^{20}$ [We define $\chi$ for ligand L , beginning with the $\mathrm{A}_{1}$ carbonyl stretching frequency ( $v_{\mathrm{co}}$ in units of $\mathrm{cm}^{-1}$ ) for $\mathrm{LNi}(\mathrm{CO})_{3}$ minus the constant value, $2056.1 \mathrm{~cm}^{-1}$. Then we divide this difference by $1 \mathrm{~cm}^{-1}$ in order to produce a dimensionless $\chi$ value.] $\theta$ is the cone angle of the phosphine, ${ }^{46} \theta_{\text {st }}$ is the steric threshold ${ }^{47}$ (the cone angle at which there is a change in the steric effect), $\lambda$ is a switching function that turns on the second steric effect after $\theta$ exceeds $\theta_{\mathrm{st}}$, and $E_{\text {ar }}$ is the aryl effect parameter, ${ }^{23}$ which depends only on the
number of aryl groups attached to the phosphine. Using eqn. (1), we have correlated (median $r^{2}=0.975$ ) over two hundred sets of thermodynamic data ( $\mathrm{p} K_{\mathrm{a}}$ values, equilibrium constants, $\Delta H^{\circ}$ and $\Delta S^{\circ}, E^{\circ}$ values), kinetic ( $\log k, \Delta H^{\ddagger}$ and $\Delta S^{\ddagger}$, product distributions, stereoselectivities), spectroscopic (IR, UV/VIS, NMR, ionization potentials) and structural (bond lengths) data. ${ }^{29,32,37,39-43,48}$ In addition, we have found that the QALE parameters $\left(\chi, \theta, E_{\mathrm{ar}}\right)$ are transferable to other groups and ligands including silyl, ${ }^{26,27}$ arsines, ${ }^{49}$ alkyl, ${ }^{49}$ nitriles, ${ }^{31}$ amines ${ }^{49}$ and thioethers. ${ }^{25,30}$

Recently, we have been studying the isoequilibrium behavior of the formal reduction potentials ( $E^{\circ}$ values) of the $\eta-\mathrm{Cp}(\mathrm{CO})$ ( L ) $\mathrm{Fe}(\mathrm{COMe})^{+10}\left[\mathrm{Cp}=\right.$ cyclopentadienyl, $\mathrm{L}=\mathrm{PR}_{3}$ and $\mathrm{P}\left(p-\mathrm{XC}_{6}{ }^{-}\right.$ $\left.\mathrm{H}_{4}\right)_{3}$ ] couple. These $E^{\circ}$ values can be measured easily, accurately, and precisely over a large range of temperature. We have focused on the variation of the structure of the very common and important ancillary phosphine ligands since these ligands have almost continuously variable stereoelectronic properties. In our initial paper ${ }^{21}$ on isoequilibrium behavior, we reported that these $E^{\circ} / T$ data (equivalent to $\Delta G^{\circ} / T$ ) exhibit distinct isoequilibrium behavior for $\mathrm{PR}_{3}$ and $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ ligands. (We take this behavior to define a family of ligands or substituents.) Since the observation of isoequilibrium behavior indicates that the property is responding to a single stereoelectronic parameter then the $E^{\circ}$ values for $\mathrm{PR}_{3}$ and $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ must be responding to different parameters. This is understandable in terms of the QALE model: ${ }^{21,22}$ Variations of $\Delta G^{\circ}$ for $\mathrm{P}\left(p-\mathrm{XC}_{6}{ }^{-}\right.$ $\left.\mathrm{H}_{4}\right)_{3}$ depend only on single parameter, $\chi$, since the other QALE parameters, $\theta$ and $E_{\text {ar }}$, are constant. $\Delta G^{\circ}$ for $\mathrm{PR}_{3}$ depends on both $\chi$ and $\theta$ but these two parameters are linearly related so that in effect $\Delta G^{\circ}$ can appear to depend on either $\chi$ or $\theta$ alone.

These results led us to the realization that with a large enough set of $\Delta H^{\circ}$ and $\Delta S^{\circ}$ values, it would be possible to choose numerous families of ligands that exhibit isoequilibrium behavior. There is no reason why the ligands in a family need to possess any particular structural relationship. The question then arises as to how the QALE model would account for these families of ligands in general, and what fundamental information can be gleaned from analysis of these families. Accordingly, we enlarged the set of $E^{\circ} / T$ data for the $\eta-\mathrm{Cp}(\mathrm{CO})$ ( L$) \mathrm{Fe}(\mathrm{COMe})^{+10}$ couple to include data for eleven complexes containing the mixed alkyl phenyl phosphines, $\mathrm{PPh}_{i} \mathrm{R}_{3-i}(i=1$,

Table 1 List of $E^{\circ} / T$ values for the $\eta-\mathrm{Cp}(\mathrm{CO})(\mathrm{L}) \mathrm{Fe}(\mathrm{COMe})^{+/ 0}$ couple and $\Delta S^{\circ}$ and $\Delta H^{\circ}$ of reduction. Data in italics are taken from ref. 52. Remaining data are reported for the first time in this paper. The standard errors of $\Delta S^{\circ}$ and $\Delta H^{\circ}$ are shown

|  | Ligand |  |  | $\left(-E^{\circ} / T\right) / 10^{-3} \mathrm{~V} \mathrm{~K}^{-1 a}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$ | $\mathrm{kJ} \mathrm{mol}{ }^{-1}$ | 229 K | 252 K | 264 K | 273 K | 293 K |
| 1 | $\mathrm{PMe}_{3}$ | $1.8 \pm 0.1$ | $35.0 \pm 0.3$ | 1.568 | 1.419 | 1.355 | 1.310 | 1.223 |
| 2 | $\mathrm{PPhMe}{ }_{2}$ | $-4.7 \pm 1.2$ | $29.5 \pm 0.3$ | 1.383 | 1.262 | 1.208 | 1.172 | 1.090 |
| 3 | $\mathrm{PEt}_{3}$ | $3.0 \pm 1.7$ | $38.7 \pm 0.5$ | 1.720 | 1.565 | 1.485 | 1.441 | 1.338 |
| 4 | $\mathrm{PBu}_{3}$ | $0.3 \pm 1.6$ | $38.6 \pm 0.5$ | 1.743 | 1.578 | 1.514 | 1.459 | 1.361 |
| 5 | $\mathrm{PPh}_{2} \mathrm{Me}$ | $-12.4 \pm 3.3$ | $23.0 \pm 0.1$ | 1.167 | 1.072 | 1.030 | 1.001 | 0.940 |
| 6 | $\mathrm{PPhEt}_{2}$ | $-6.9 \pm 1.1$ | $31.5 \pm 0.3$ | 1.495 | 1.364 | 1.309 | 1.267 | 1.183 |
| 7 | $\mathrm{PPhBu}_{2}$ | $-4.7 \pm 1.2$ | $32.7 \pm 0.3$ | 1.524 | 1.394 | 1.331 | 1.289 | 1.201 |
| 8 | $\mathrm{PPh}_{2} \mathrm{Et}$ | $-14.9 \pm 0.6$ | $24.2 \pm 0.1$ | 1.253 | 1.155 | 1.108 | 1.076 | 1.014 |
| 9 | $\mathrm{PPh}_{2} \mathrm{Pr}$ | $-10.9 \pm 0.6$ | $25.5 \pm 0.2$ | 1.266 | 1.162 | 1.114 | 1.081 | 1.014 |
| 10 | $\mathrm{PPh}_{2} \mathrm{Bu}$ | $-13.8 \pm 0.1$ | $24.7 \pm 0.4$ | 1.258 | 1.155 | 1.111 | 1.082 | 1.017 |
| 11 | $P B u^{i}{ }_{3}$ | $2.2 \pm 1.8$ | $38.5 \pm 0.5$ | 1.719 | 1.553 | 1.486 | 1.436 | 1.339 |
| 12 | $\mathrm{P}\left(\mathrm{p}-\mathrm{MeOC}_{6} \mathrm{H}_{4}\right)_{3}$ | $-22.2 \pm 0.7$ | $23.1 \pm 0.2$ | 1.273 | 1.178 | 1.133 | 1.105 | 1.105 |
| 13 | $P\left(p-\mathrm{Me}_{6} \mathrm{H}_{4}\right)_{3}$ | $-18.5 \pm 1.8$ | $22.6 \pm 0.6$ | 1.217 | 1.116 | 1.078 | 1.050 | 0.9934 |
| 14 | $\mathrm{PPh}_{3}$ | $-16.6 \pm 1.7$ | $20.5 \pm 0.5$ | 1.098 | 1.019 | 0.9729 | 0.9482 | 0.8972 |
| 15 | $P\left(p-F C_{6} H_{4}\right)_{3}$ | $-13.2 \pm 1.2$ | $16.9 \pm 0.3$ | 0.9025 | 0.8293 | 0.8018 | 0.7805 | 0.7338 |
| 16 | $\mathrm{P}\left(\mathrm{p}-\mathrm{ClC}_{6} \mathrm{H}_{4}\right)_{3}$ | $-7.3 \pm 1.7$ | $16.2 \pm 0.5$ | 0.8108 | 0.7385 | 0.7091 | 0.6890 | 0.6515 |
| 17 | $P\left(P-F_{3} \mathrm{CC}_{6} \mathrm{H}_{4}\right)_{3}$ | $-6.0 \pm 2.2$ | $11.7 \pm 0.6$ | 0.5966 | 0.5390 | 0.5224 | 0.5071 | 0.4800 |
| 18 | $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ | $-4.18 \pm 1.5$ | $46.3 \pm 0.1$ | 2.136 | 1.947 | 1.858 | 1.803 | 1.677 |
| 19 | $\mathrm{PPh}_{2} \mathrm{Pr}^{\mathrm{i}}$ | $-8.8 \pm 0.1$ | $28.5 \pm 0.2$ | 1.380 | 1.263 | 1.208 | 1.171 | 1.100 |
| 20 | $\mathrm{PPh}_{2} \mathrm{Cy}$ | $-9.4 \pm 1.1$ | $29.1 \pm 0.3$ | 1.417 | 1.294 | 1.239 | 1.206 | 1.128 |
| 21 | $\mathrm{PPhPr}^{\mathrm{i}}{ }_{2}$ | $-14.2 \pm 0.7$ | $31.1 \pm 0.2$ | 1.557 | 1.427 | 1.369 | 1.330 | 1.251 |
| 22 | $\mathrm{PPr}^{\text {i }}{ }_{3}$ | $2.1 \pm 0.8$ | $43.0 \pm 0.2$ | 1.917 | 1.742 | 1.662 | 1.606 | 1.495 |
| 23 | $\mathrm{PPhCy}_{2}$ | $-14.7 \pm 1.4$ | $32.9 \pm 0.4$ | 1.637 | 1.505 | 1.443 | 1.402 | 1.314 |
| 24 | $\mathrm{PCy}_{3}$ | $-1.8 \pm 1.4$ | $44.0 \pm 0.4$ | 2.006 | 1.827 | 1.746 | 1.690 | 1.571 |

${ }^{a} E^{\circ}$ measured by cyclic voltammetry relative to the acetylferrocenium/acetylferrocene couple in acetonitrile. The error in $E^{\circ}$ is estimated to be 0.7 mV .

2; $\mathrm{R}=\mathrm{Me}, \mathrm{Et}, \operatorname{Pr}\left(i=2\right.$ only), $\left.\mathrm{Bu}, \mathrm{Pr}^{\mathrm{i}}, \mathrm{Cy}\right)$. This set of data when combined with the previously reported data for $\mathrm{PR}_{3}$ and $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ does indeed show many families of ligands that exhibit isoequilibrium behavior.

In this paper, we show that isoequilibrium (and isokinetic) behavior may result from a system responding not to a single stereoelectronic parameter but to a linear combination of $n-1$ stereoelectronic parameters where $n$ is the total number of fundamental parameters needed to describe the system. We then present a methodology based on isoequilibrium behavior for $n=3$ that allows us to determine this linear combination of two stereoelectronic properties and to evaluate them individually. We then test this methodology by calculating the $\chi$ values of $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$. Since Bartik $^{20}$ has already reported $\chi$ values for a number of $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$, we have a set of values with which to compare our results. We extended this study to the (previously unreported) stereoelectronic properties of tris(pyrrolidinyl)phosphine, $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$. This strong electron donor ligand is considered to be isosteric with $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$, so that determination of its $\chi$ and $E_{\text {ar }}$ values would make it useful for ligand effect studies. ${ }^{50}$

## Results and discussion

The $\eta-\mathrm{Cp}(\mathrm{CO})(\mathrm{L})(\mathrm{COMe}) \mathrm{Fe}^{+/ 0}$ couple is a remarkably wellbehaved system suitable for systematic and quantitative studies of ligand effects. The complexes are readily prepared ${ }^{51}$ and the stereoelectronic properties of phosphorus(III) ligands are almost continuously variable. ${ }^{46}$
$\eta-\mathrm{Cp}(\mathrm{CO})(\mathrm{L}) \mathrm{Fe}(\mathrm{COMe})+\mathrm{e} \underset{\eta-\mathrm{Cp}(\mathrm{CO})(\mathrm{L}) \mathrm{Fe}(\mathrm{COMe})}{\rightleftharpoons}$
The system is chemically reversible and electrochemically quasireversible. We have been able to measure accurately and precisely $E^{\circ} / T$ values for this system relative to the acetylferrocinium/acetylferrocene couple at five temperatures over a range of 60 K . These data are listed in Table 1. Each measure-


Fig. 1 Plot of $E^{\circ} / T$ versus $\chi$ for all the ligands displayed in Table 1.
ment was repeated five to ten times at each of the five temperatures. The error in our measurements is less than 0.7 mV , which is more than adequate for our studies. We established the validity of the reported $E^{\circ}$ value by computer simulation methods. There is no evidence of any follow-up reactions, there is no deposition on the electrodes and finally the plots of $E^{\circ} / T$ versus $1 / T$ are linear ( $r^{2}=0.999$ ) over a range of $60^{\circ} \mathrm{C}$. From the slopes and intercepts of the plots of $E^{\circ} / T$ versus $1 / T$ we obtained the $\Delta H^{\circ}$ and $\Delta S^{\circ}$ of reduction, which are displayed in Table 1. The errors in $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are presented in Table 1.

We summarize the results of our study in a plot of $E^{\circ} / T$ versus $1 / T$ (Fig. 1) for all the ligands displayed in Table 1. Although there are several families of ligands (sets of ligands that exhibit isoequilibrium behavior) buried in this plot [e.g. $\mathrm{PR}_{3}$ and $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ ], these points of intersection are obscured by the complexity of the graph.

To clarify the situation, we turn to the corresponding plot of $\Delta H^{\circ}$ versus $\Delta S^{\circ}$ and look for any series of three or more points that lie on a straight line (Fig. 2). For these ligands, $\Delta H^{\circ}$ is


Fig. 2 A plot of $\Delta H^{\circ}$ versus $\Delta S^{\circ}$ for the reduction of $\eta-\mathrm{Cp}(\mathrm{CO})-$ $(\mathrm{L}) \mathrm{Fe}(\mathrm{COMe})^{+}$. The solid line is drawn through the points for $\mathrm{P}\left(p-\mathrm{MeC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PPh}_{2} \mathrm{Cy}, \mathrm{PPhEt}_{2}, \mathrm{PPhBu}_{2}, \mathrm{PBu}_{3}{ }_{3}$ and $\mathrm{PEt}_{3}$.
linearly related to $\Delta S^{\circ}$, a necessary condition that the ligands form a family. In Fig. 2, a family $\left[\mathrm{P}\left(p-\mathrm{MeC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PPh}_{2} \mathrm{Cy}\right.$, $\mathrm{PPhEt}_{2}, \mathrm{PPhBu}_{2}, \mathrm{PBu}_{3}{ }_{3}$, and $\mathrm{PEt}_{3}$ ] is identified and in Fig. 3 this family membership is confirmed by the observation of a fan shaped array of lines in the $E^{\circ} / T$ versus $1 / T$ plot. This set of data passes Linert's first $F$ test ${ }^{11,53}$ but not the second. The second $F$ test is extremely rigorous and few systems pass both of them. Nevertheless, Linert maintains that passage of the first $F$ test is very good evidence that the point of intersection exists. ${ }^{8}$ Other families are readily found.

The set of ligands that form the family shown in Fig. 3 do not have any special structural relationship other than being phosphines. The question arises as to how they can form a family if $E^{\circ} / T$ must respond to only a single parameter. As we will see the $E^{\circ} / T$ values for this family do respond to an 'effectively single' parameter but this parameter is a linear combination of two QALE parameters.

In the following discussion, we show the general requirement for a set of ligands to form a family, i.e. they exhibit isoequilibrium behavior. We start with the assumption that $\Delta G^{\circ}$ is linearly related to the variation in the stereoelectronic properties of a set of ligands [eqn. (3)]. We restrict our attention to a

$$
\begin{equation*}
\Delta G^{\circ}=a \chi+b \theta+c E_{\mathrm{ar}}+d \tag{3}
\end{equation*}
$$

three parameter system with no steric threshold. For convenience we use the three QALE parameters $\chi, \theta$ and $E_{\mathrm{ar}}$, where the coefficients $a, b$ and $c$ are characteristic of the system being studied. These coefficients are temperature dependent and this dependence is shown explicitly in eqn. (4).

$$
\begin{equation*}
\Delta G^{\circ}=\Delta H^{\circ}-T \Delta S^{\circ} \tag{4}
\end{equation*}
$$

Since $\Delta G^{\circ}$ can be expressed in terms of a linear combination of parameters [eqn. (3)] then its components, $\Delta S^{\circ}$ and $\Delta H^{\circ}$, must also be related to the same QALE parameters via eqns. (5) and (6).

$$
\begin{align*}
& \Delta H^{\circ}=a_{1} \chi+b_{1} \theta+c_{1} E_{\mathrm{ar}}+d_{1}  \tag{5}\\
& \Delta S^{\circ}=a_{2} \chi+b_{2} \theta+c_{2} E_{\mathrm{ar}}+d_{2} \tag{6}
\end{align*}
$$

We assume that the coefficients of eqns. (5) and (6) are temperature independent over the experimental range of temperature. We conclude that $\Delta H^{\circ}$ is linearly related to $\Delta S^{\circ}$ since the plot of $\Delta G^{\circ} / T$ versus $1 / T$ is fan shaped [eqn. (7)]. $\beta$ is the temperature of the intersection point of the fan-shaped array of


Fig. 3 A plot of $E^{\circ} / T$ versus $1 / T$ for the ligands $\mathrm{P}\left(p-\mathrm{MeC}_{6} \mathrm{H}_{4}\right)_{3}$, $\mathrm{PPh}_{2} \mathrm{Cy}, \mathrm{PPhEt}_{2}, \mathrm{PPhBu}_{2}, \mathrm{PBu}_{3}{ }_{3}$ and $\mathrm{PEt}_{3}$ (in descending order on the right side of the plot).
lines for a given family, and $\Delta G_{\beta}^{\circ}$ is the value of $\Delta G^{\circ}$ at the intersection point. On combining eqns. (5)-(7) and solving for $E_{\mathrm{ar}}$, we get eqn. (8).

$$
\begin{gather*}
\Delta H^{\circ}=\beta \Delta S^{\circ}+\Delta G_{\beta}^{\circ}  \tag{7}\\
E_{\mathrm{ar}}=\frac{\left(\beta a_{2}-a_{1}\right) \chi+\left(\beta b_{2}-b_{1}\right) \theta+\left(\Delta G_{\beta}^{\circ}+\beta d_{2}-d_{1}\right)}{c_{1}-\beta c_{2}} \tag{8}
\end{gather*}
$$

We substitute this expression for $E_{\text {ar }}$ into eqns. (5) and (6). On collecting terms in $\chi$ and $\theta$, we get expressions for $\Delta H^{\circ}$ and $\Delta S^{\circ}$ [eqns. (9) and (10)]. where $p, A, B$ and $C$ are given by eqns. (11)(14).

$$
\begin{gather*}
\Delta H^{\circ}=\beta A(\chi+p \theta)+B  \tag{9}\\
\Delta S^{\circ}=A(\chi+p \theta)+C  \tag{10}\\
p=\frac{b_{2} c_{1}-b_{1} c_{2}}{a_{2} c_{1}-a_{1} c_{2}}  \tag{11}\\
A=\frac{a_{2} c_{1}-a_{1} c_{2}}{c_{1}-\beta c_{2}}  \tag{12}\\
B=\frac{\beta\left(d_{2} c_{1}-d_{1} c_{2}\right)+c_{1} \Delta G_{\beta}^{\circ}}{a_{2} c_{1}-a_{1} c_{2}}  \tag{13}\\
C=\frac{d_{2} c_{1}-d_{1} c_{2}+c_{2} \Delta G_{\beta}^{\circ}}{a_{2} c_{1}-a_{1} c_{2}} \tag{14}
\end{gather*}
$$

$A$ and $B$ depend on the isoequilibrium temperature $\beta$, thus, are constant within a family but vary from family to family. Thus, we see that, in general, both $\Delta S^{\circ}$ and $\Delta H^{\circ}$ for a family are expressible in terms of a single variable $z_{3}$ [eqn. (15)], which is a

$$
\begin{equation*}
z_{3}=\chi+p \theta \tag{15}
\end{equation*}
$$

composite of $\chi$ and $\theta$. The symbol $z_{3}$ designates that this composite parameter is derived for a three parameter model. Or put another way, $\Delta H^{\circ}$ and $\Delta S^{\circ}$ for a family must each be linearly related to $z_{3}$, which is not one of the three fundamental stereoelectronic parameters in the model. Thus, the observation of isoequilibrium (or isokinetic) behavior does not necessarily mean that $\Delta G^{\circ}$ is responding to variations in a single fundamental stereoelectronic parameter. Because of the single relationship [eqn. (7)] relating $\Delta H^{\circ}$ and $\Delta S^{\circ}$ for a fan-shaped array of lines, we see that for an ' $n$ ' parameter system the 'effect-

Table 2 Values of $z_{3}$ and $\chi_{z}$ calculated as described in the text using the ligands listed under the heading 'Source'. We estimate that the standard error in $\chi_{z}$ is $\pm 1.0$

|  | Ligand | $z_{3}$ | $\chi_{z}{ }^{a}$ | Source |
| :---: | :---: | :---: | :---: | :---: |
| 1 | PPhMe 2 | 13.9 | 10.5 | $\mathrm{P}\left(\mathrm{C}_{6} \mathrm{H}_{5}\right)_{3}$ and $\mathrm{PMe}_{3}$ |
| 2 | PPhMe 2 | 13.8 | 10.4 | $\mathrm{P}\left(p-\mathrm{ClC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PCy}_{3}$ |
| 3 | $\mathrm{PPh}_{2} \mathrm{Me}$ | 16.4 | 12.6 | $\mathrm{P}\left(\mathrm{C}_{6} \mathrm{H}_{5}\right)_{3}$ and $\mathrm{PMe}_{3}$ |
| 4 | $\mathrm{PPh}_{2} \mathrm{Me}$ | 16.4 | 12.6 | $\mathrm{P}\left(p-\mathrm{ClC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PPh}_{2} \mathrm{Bu}$ |
| 5 | $\mathrm{PPhEt}_{2}$ | 12.4 | 8.6 | $\mathrm{P}\left(p-\mathrm{FC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PCy}_{3}$ |
| 6 | $\mathrm{PPhEt}_{2}$ | 12.5 | 8.7 | $\mathrm{P}\left(p-\mathrm{MeC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PEt}_{3}$ |
| 7 | $\mathrm{PPhEt}_{2}$ | 12.4 | 8.6 | $\mathrm{P}\left(p-\mathrm{MeC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PEt}_{3}, \mathrm{PBu}_{3}^{\mathrm{i}}$ |
| 8 | $\mathrm{PPhBu}_{2}$ | 11.8 | 7.9 | $\mathrm{PPh}_{3}, \mathrm{PCy}_{3}$ |
| 9 | $\mathrm{PPhBu}_{2}$ | 11.8 | 7.9 | $\mathrm{PPh}_{2} \mathrm{Me}, \mathrm{PBu}_{3}$ |
| 10 | $\mathrm{PPhBu}_{2}$ | 12.2 | 8.3 | $\mathrm{PPh}_{2} \mathrm{Et}, \mathrm{PEt}_{3}$ |
| 11 | $\mathrm{PPhBu}_{2}$ | 12.1 | 8.2 | $\mathrm{P}\left(p-\mathrm{MeOC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PPhEt}_{2}$ |
| 12 | $\mathrm{PPhBu}_{2}$ | 11.9 | 8.0 | $\mathrm{P}\left(p-\mathrm{MeC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PPh}_{2} \mathrm{Cy}$ |
| 13 | $\mathrm{PPhBu}_{2}$ | 12.0 | 8.2 | $\mathrm{P}\left(p-\mathrm{F}_{3} \mathrm{CC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PPhMe} 2$ |
| 14 | $\mathrm{PPh}_{2} \mathrm{Et}$ | 14.9 | 10.9 | $\mathrm{PPh}_{2} \mathrm{Cy}, \mathrm{PPhEt}_{2}$ |
| 15 | $\mathrm{PPh}_{2} \mathrm{Et}$ | 15.0 | 11.1 | $\mathrm{PPh}_{2} \mathrm{Pr}^{\mathrm{i}}, \mathrm{PMe}_{3}$ |
| 16 | $\mathrm{PPh}_{2} \mathrm{Et}$ | 15.2 | 11.2 | $\mathrm{P}\left(p-\mathrm{MeC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PPhMe}_{2}$ |
| 17 | $\mathrm{PPh}_{2} \mathrm{Pr}$ | 15.2 | 11.2 | $\mathrm{PPh}_{2} \mathrm{Me}, \mathrm{PBu}_{3}$ |
| 18 | $\mathrm{PPh}_{2} \mathrm{Pr}$ | 15.2 | 11.2 | $\mathrm{PPh}_{2} \mathrm{Pr}^{\mathrm{i}}, \mathrm{PPhEt}_{2}$ |
| 19 | $\mathrm{PPh}_{2} \mathrm{Bu}$ | 15.3 | 11.3 | $\mathrm{PPh}_{3}, \mathrm{PCy}_{3}$ |
| 20 | $\mathrm{PPh}_{2} \mathrm{Bu}$ | 15.3 | 11.3 | $\mathrm{PPh}_{2} \mathrm{Cy}, \mathrm{PPhEt}_{2}, \mathrm{PBu}_{3}$ |
| 21 | $\mathrm{PPh}_{2} \mathrm{Pr}^{\text {i }}$ | 13.8 | 9.6 | $\mathrm{P}\left(p-\mathrm{MeC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PMe}_{3}$ |
| 22 | $\mathrm{PPh}_{2} \mathrm{Pr}^{\mathrm{i}}$ | 13.8 | 9.6 | $\mathrm{PPh}_{2} \mathrm{Me}, \mathrm{PPh}_{2} \mathrm{Pr}$ |
| 23 | $\mathrm{PPh}_{2} \mathrm{Cy}$ | 13.2 | 8.9 | $\mathrm{P}\left(p-\mathrm{MeC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PEt}_{3}, \mathrm{PBu}_{3}^{\mathrm{i}}$ |
| 24 | $\mathrm{PPh}_{2} \mathrm{Cy}$ | 13.4 | 9.1 | $\mathrm{PPh}_{2} \mathrm{Me}, \mathrm{PCy}_{3}$ |
| 25 | $\mathrm{PPh}_{2} \mathrm{Cy}$ | 13.7 | 9.4 | $\mathrm{PPh}_{3}, \mathrm{PPr}_{3}^{\mathrm{i}}$ |
| 26 | $\mathrm{PPh}_{2} \mathrm{Cy}$ | 13.2 | 8.9 | $\mathrm{P}\left(p-\mathrm{MeOC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PMe}_{3}$ |
| 27 | $\mathrm{PPh}^{\text {Pr }}{ }_{2}$ | 11.3 | 7.0 | $\mathrm{P}\left(p-\mathrm{MeOC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PCy}_{3}$ |
| 28 | $\mathrm{PPhPr}_{2}{ }_{2}$ | 11.6 | 7.2 | $\mathrm{P}\left(p-\mathrm{FC}_{6} \mathrm{H}_{4}\right)_{2}, \mathrm{PPh}_{2} \mathrm{Bu}$ |
| 29 | $\mathrm{PPhCy}_{2}$ | 10.6 | 6.1 | $\mathrm{P}\left(p-\mathrm{FC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PPh}_{2} \mathrm{Bu}$ |
| 30 | $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ | 4.5 | 0.4 | $\begin{aligned} & \mathrm{PPh}_{2} \mathrm{Me}, \mathrm{PPh}_{2} \mathrm{Pr}, \mathrm{PPh}_{2} \mathrm{Cy}, \\ & \mathrm{P}\left(p-\mathrm{FC}_{6} \mathrm{H}_{4}\right)_{3} \end{aligned}$ |
| 31 | $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ | 4.5 | 0.4 | $\mathrm{PEt}_{3}, \mathrm{PCy}_{3}$ |

${ }^{a}$ We treat the $\chi$ and $\chi_{z}$ values as dimensionless parameters defined by $\chi(\exp ) / 1 \mathrm{~cm}^{-1}$.
ively single' parameter can be made up of a linear combination of a maximum of $n-1$ parameters.

Eqns. (9) and (15) give us a way to determine values of $\chi$ and $E_{\text {ar }}$ for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ that is very different from previous methods We show that for this particular system the values of $z_{3}$ are not very sensitive to the actual value of the cone angle, $\theta$. Furthermore, evaluation of $z_{3}$ is independent of the actual values of $E_{\text {ar }}$ for the individual $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$. To calculate the $\chi$ values for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ we need the values of the coefficients $a_{1}$ through $d_{2}$ in eqns. (5) and (6). For this purpose, we used the ligands $\mathrm{PR}_{3}$ and $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$, whose QALE parameters (Table 2) are known. We then analyzed their $\Delta H^{\circ}$ and $\Delta S^{\circ}$ (Table 1) values via regression analysis using eqns. (5) and (6). We note for $\Delta H^{\circ}$ that there is a negligible contribution from $\theta$, which is statistically indistinguishable from zero [eqn. (16)]. (The percent contribution of

$$
\begin{gather*}
\Delta H^{\circ}=-(1.16 \pm 0.08) \chi+(0.023 \pm 0.018) \theta- \\
\quad(3.72 \pm 0.31) E_{\mathrm{ar}}+42 \pm 2.8  \tag{16}\\
n=12 \quad r^{2}=0.998 \\
\chi=66 \% \quad \theta=4 \% \quad E_{\mathrm{ar}}=30 \%
\end{gather*}
$$

a parameter to the property was determined by first multiplying the absolute value of the coefficient of the parameter by the range of the parameter. Then the result was divided by the sum of all the products of coefficient times range.) Hence, we performed the analysis of $\Delta H^{\circ}$ in terms of $\chi$ and $E_{\text {ar }}$ only [eqn. (17)]. (Note that here is a case where removal of a

$$
\begin{align*}
& \Delta H^{\circ}= \\
& \quad-(1.21 \pm 0.07) \chi-(3.51 \pm 0.28) E_{\mathrm{ar}}+45.8 \pm 0.4  \tag{17}\\
& n=12 \quad r^{2}=0.997
\end{align*}
$$

parameter leads to better statistics in terms of smaller standard
errors.) Eqn. (17) gives the values of $a_{1}$ and $c_{1}$ that we will use in calculating ' $p$ ' in eqn. (11).

The values of $a_{2}, b_{2}$ and $c_{2}$ needed for the calculation of ' $p$ ' come from the regression analysis of $\Delta S^{\circ}$ for the $12 \mathrm{PR}_{3}$ and $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ [eqn. (18)].

$$
\begin{align*}
\Delta S^{\circ}=(1.65 \pm 0.20) \chi+ & (0.16 \pm 0.05) \theta- \\
& (11.6 \pm 0.8) E_{\mathrm{ar}}-29.8 \pm 7.2  \tag{18}\\
n= & 12 \quad r^{2}=0.976
\end{align*}
$$

Using the appropriate values of the coefficients we get a value for ' $p$ ' [eqn. (19)]. We note that the contribution of $p \theta$ to $z_{3}$ is

$$
\begin{equation*}
p=0.028 \pm 0.013 \tag{19}
\end{equation*}
$$

small. For example, in the $\mathrm{PPh}_{i} \mathrm{Me}_{3-i}$ family (vide infra), the variation of $p \theta$ is around $14 \%$ of the variation of $z_{3}$.

In the following examples we show how we determine the $\chi$ and $E_{\text {ar }}$ values for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$. One might expect family membership to be shown by a set of ligands, $\mathrm{PPh}_{i} \mathrm{R}_{3-i}(i=1,2,3)$ on the basis of their structural relationships. In other words, we might assume that $\chi, \theta$ and $E_{\text {ar }}$ would be linear functions of the index ' $i$ '. Formally, one would then describe these stereoelectronic parameters as being parametrically related or simply as showing the property of additivity. More generally, the label ' $i$ ' can be left out of the picture and the parametric (family) relationship would arise from $\theta$, and $E_{\text {ar }}$, being linear functions of $\chi$. In either case, a plot of $E^{\circ} / T$ versus $1 / T$ for the set $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ is expected to form a fan-shaped array of four lines. Fig. 4 shows such plots for $R=\mathrm{Me}, \mathrm{Et}, \mathrm{Bu}, \mathrm{Pr}^{\mathrm{i}}$ and Cy . Indeed, we see for the first three sets the expected fan-shaped arrays. The last two sets form a fan-shaped array with three of their members, but the fourth turns out not to be a member of the family. As pointed earlier, all of these experimental results have been checked five to ten times with freshly prepared materials and found to be reproducible. We believe that these results indicate, first, that our method is capable of good accuracy; second, that the deviant ligands in the last two sets are truly not family members of their sets, but they might be (and are) members of families that show no particular structural relationships among their members. Recall that family membership requires only that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are expressible in terms of an effectively single parameter. In contrast to structurally related families, this parameter for a structurally unrelated family is not a single fundamental stereoelectronic parameter, but rather is a linear combination of one fewer stereoelectronic parameters than the number required to describe the total group of ligands under study (vide supra). In the present study, three parameters $(\chi, \theta$ and $E_{\mathrm{ar}}$ ) are required, thus the general effectively single variable is a linear combination of any pair of these; we have chosen the pair to be $\chi$ and $\theta$. We note that for a special case of a structurally related family, the effectively single parameter is still valid, it merely collapses to a single fundamental stereoelectronic parameter.

We are now ready to calculate the values of $\chi$ for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ based on their isoequilibrium behavior. We know the values of $\chi$ and $\theta$ for $\mathrm{PMe}_{3}$ and $\mathrm{PPh}_{3}$, thus, we know their values of $z_{3}$. We make a plot of $z_{3}$ versus $\Delta H^{\circ}$ for these two ligands and use this plot as a calibration curve to determine the $z_{3}$ values of the $\mathrm{PPh}_{2} \mathrm{Me}$ and $\mathrm{PPhMe} 2_{2}$ whose $\Delta H^{\circ}$ values are known (Table 1). Using eqn. (15) we convert the $z_{3}$ values back to $\chi_{z}$ (the subscript ' $z$ ' to designate that these $\chi$ values are derived from $z_{3}$ ). In a similar manner, we find other families that contain at least one $\mathrm{PPh}_{i} \mathrm{R}_{3-i}, \mathrm{PR}_{3}$ and $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ ligand. For each family we calculate the $z_{3}$ values of a particular $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ ligand. For a few ligands (e.g. $\mathrm{PPhCy}_{2}$ ) that do not fall on lines that connect $\mathrm{PR}_{3}$ and $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$, we found that these ligands form families with other $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ whose $z_{3}$ values were determined previously.


Fig. 4 Plots of $E^{\circ} / T$ versus $1 / T$ for (A) $\mathrm{PPh}_{i} \mathrm{Me}_{3-i}$, (B) $\mathrm{PPh}_{i} \mathrm{Et}_{3-i}$, (C) $\mathrm{PPh}_{i} \mathrm{Bu}_{3-i}$, (D) $\mathrm{PPh}_{i} \mathrm{Pr}_{3-i}{ }_{3}$, (E) $\mathrm{PPh}_{i} \mathrm{Cy}_{3-i}$. The observation of isoequilibrium confirms family membership for (A)-(C). Thus, plots of $\Delta H^{\circ}$ or $S^{\circ}$ versus $z_{3}$ for this family should be linear. In (D) and (E), the dashed lines correspond to the data for $\mathrm{PPhPr}_{2}^{\mathrm{i}}$ and $\mathrm{PPhCy}_{2}$, respectively.

We illustrate this protocol in Fig. 5 where we show the families to which $\mathrm{PPh}_{2} \mathrm{Cy}$ belongs. We also show the $E^{\circ} / T$ versus $1 / T$ plots which we use to confirm the family membership. In Table 2, we present the $z_{3}$ values, calculated using different sets of ligands, for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ and their corresponding calculated $\chi_{z}$ values. We present in Table 3 the average values of $z_{3}$ and $\chi_{z}$. We estimate that the error in $\chi_{z}$ is $\pm 1.0$.

We noted earlier that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are both linearly related to $z_{3}$ for a family of ligands. In Fig. 6, we illustrate that this is indeed the case for the family of ligands presented in Figs. 2 and 3.

We note that the $\chi_{z}$ values that we calculate, in general, do not deviate greatly from the Bartik $\chi$ values (Table 2, Fig. 7). The one exception is $\mathrm{PPh}_{2} \mathrm{Pr}^{\mathrm{i}}$ for which our calculated $\chi_{z}$ value is 9.6 in comparison to the Bartik ${ }^{20}$ value of 10.85 . Our value is closer to the additive value of 10.0. (Bartik did not report $\chi$ values for $\mathrm{PPhCy}_{2}$ or $\mathrm{PPh}_{2} \mathrm{Cy}$.)

We next examine the $E_{\text {ar }}$ values for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$. A plot of $\Delta H^{\circ}$ versus $\chi$ (either the new values reported herein or Bartik's values) show considerable scatter for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ (Fig. 8). This is unexpected if the $E_{\mathrm{ar}}$ values of $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ were 1 and 2 for $i=1$ and 2 , respectively. In this case the expected plot should show three nearly equally spaced parallel lines for $\mathrm{PR}_{3}, \mathrm{PPhR}_{2}$, and
$\mathrm{PPh}_{2} \mathrm{R}$. We interpret this to mean that one of the stereoelectronic parameters is incorrectly defined. The problem cannot be $\theta$ since $\Delta H^{\circ}$ is not very sensitive to $\theta$. We can also eliminate $\chi$ since this parameter was calculated in a manner that did not depend on $E_{\text {ar }}$ of the mixed alkyl phenyl ligands and only weakly on $\theta$ through eqn. (15) ( $\theta$ would have to vary over an unrealistic range to produce this scatter). In addition, our calculated $\chi$ values agree well with Bartik's values. Therefore, the problem resides in $E_{\mathrm{ar}}$.

Values of $E_{\text {ar }}$ for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ are readily calculated via eqn. (17) once we have the $\chi$ values. These calculated $E_{\mathrm{ar}}$ values are listed in Table 3. We estimate that the error is $\pm 0.30$ in the $E_{\text {ar }}$ values. In the QALE model, we made the approximation that $E_{\text {ar }}$ depended only on ' $i$ ' for a $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$. Thus when $i=2, E_{\mathrm{ar}}=2$ and when $i=1, E_{\mathrm{ar}}=1$. The calculated values of $E_{\mathrm{ar}}$ are within statistical error of 2.0 for $\mathrm{PPh}_{2} \mathrm{R}$ with the exception of the isopropyl and cyclohexyl derivatives, whose $E_{\mathrm{ar}}$ values (1.5 and 1.6, respectively) are significantly less than 2 . Similarly, we find that the $E_{\mathrm{ar}}$ values for $i=1$ are close to 1.0 , with the exception of the isopropyl and cyclohexyl derivatives, whose $E_{\text {ar }}$ values (1.7 and 1.6 , respectively) are significantly larger than 1.0. These observations suggest that the $E_{\text {ar }}$ values are significantly altered by large alkyl groups. We do not yet know if this deviation of the


Fig. 5 A plot (A) of $\Delta H^{\circ}$ versus $\Delta S^{\circ}$. The lines show the families to which $\mathrm{PPh}_{2} \mathrm{Cy}$ belongs. The confirmation of family membership is shown in the plots [(B)-(E)] of $E^{\circ} / T$ versus $1 / T$ where isoequilibrium behavior is observed for each of the four families. The families of ligands are (B) $\mathrm{P}\left(p-\mathrm{MeC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PEt}_{3}, \mathrm{PBu}_{3}^{\mathrm{i}}$ (lines for $\mathrm{PEt}_{3}$ and $\mathrm{PBu}_{3}^{\mathrm{i}}$ overlap), $\mathrm{PPh}_{2} \mathrm{Cy}$; (C) $\mathrm{PPh}_{2} \mathrm{Me}, \mathrm{PCy}_{3}, \mathrm{PPh}_{2} \mathrm{Cy}$; (D) $\mathrm{PPh}_{3}, \mathrm{PPr}_{3}^{\mathrm{i}}, \mathrm{PPh} 2 \mathrm{Cy}$; (E) $\mathrm{P}\left(p-\mathrm{MeOC}_{6} \mathrm{H}_{4}\right)_{3}$, $\mathrm{PMe}_{3}, \mathrm{PPh}_{2} \mathrm{Cy}$.
$E_{\mathrm{ar}}$ values from the values of 1 or 2 is system-dependent. This situation is perplexing; its resolution might shed light on the nature of the aryl effect.

## Evaluation of the stereoelectronic parameters of $\mathbf{P}\left(\mathbf{N C}_{\mathbf{4}} \mathbf{H}_{\mathbf{8}}\right)_{3}{ }^{54}$

We have used the methodology described herein to determine the $\chi$ value for $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ based on the assumption that the stereochemical properties are adequately described by $\chi, \theta$ and $E_{\mathrm{ar}}$. The appropriate data are displayed in entries 30 and 31 in Table 2. We use $145^{\circ}$ for $\theta$ as reported by Moloy and Petersen. ${ }^{50}$ We find that $\chi=0.4 \pm 1.0$ for this ligand making it second only to $\mathrm{PBu}_{3}^{\mathrm{t}}$ in electron donor capacity. As we will show, $E_{\mathrm{ar}}=0$ for this ligand (vide infra).

Because of the particular nature of the stereoelectronic properties of $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$, it will behave at times as a $\mathrm{PR}_{3}$, a $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$, or neither depending on the nature of the system. We illustrate this behavior in the next three examples. It is important to note that with $\chi=0.4$ and $\theta=145^{\circ}$, this ligand does not share the same parametric relationship between $\chi$ and $\theta$ that is exhibited by the common $\mathrm{PR}_{3}$. Consequently, the datum for $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ will fall along the line determined by $\mathrm{PR}_{3}$ in a ' $\chi$ ' plot (Fig. 9) only when steric effects are not operative and either the aryl effect is not operative, or $E_{\text {ar }}$ is zero for this ligand. Steric effects are not operative for $\Delta H^{\circ}$ of reduction of the $\eta-\mathrm{Cp}(\mathrm{CO})(\mathrm{L}) \mathrm{Fe}(\mathrm{COMe})^{+/ 0}$ couple (vide supra), thus $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ behaves like a $\mathrm{PR}_{3}$ ligand and lies along the line defined by the $\mathrm{PR}_{3}$ ligands (Fig. 9A). Since the 'aryl effect' is

Table 3 Literature parameters and parameters calculated as described in this paper

|  | Ligand | $\theta^{a}$ | $\chi^{b}$ | $E_{\text {ar }}{ }^{c}$ | $z_{3}(\mathrm{calc})^{d}$ | $z_{3}(\mathrm{ave})^{e}$ | $\chi_{z}(\mathrm{ave})^{e}$ | $E_{\text {ar }}(z)^{e}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\mathrm{PMe}_{3}$ | 118 | 8.55 | 0 | 11.9 |  |  |  |
| 2 | PPhMe 2 | 122 | 10.6 | 1 |  | 13.9 | 10.5 | 1.0 |
| 3 | $\mathrm{PEt}_{3}$ | 132 | 6.3 | 0 | 10.0 |  |  |  |
| 4 | $\mathrm{PBu}_{3}$ | 136 | 5.25 | 0 | 9.1 |  |  |  |
| 5 | $\mathrm{PPh}_{2} \mathrm{Me}$ | 136 | 12.1 | 2 |  | 16.4 | 12.6 | 2.2 |
| 6 | $\mathrm{PPhEt}_{2}$ | 136 | 9.3 | 1 |  | 12.4 | 8.6 | 1.1 |
| 7 | $\mathrm{PPhBu}_{2}$ | 139 | 8.6 | 1 |  | 12.0 | 8.1 | 1.3 |
| 8 | $\mathrm{PPh}_{2} \mathrm{Et}$ | 140 | 11.3 | 2 |  | 15.1 | 11.1 | 2.3 |
| 9 | $\mathrm{PPh}_{2} \mathrm{Pr}$ | 141 | 11.2 | 2 |  | 15.2 | 11.2 | 1.9 |
| 10 | $\mathrm{PPh}_{2} \mathrm{Bu}$ | 142 | 11.1 | 2 |  | 15.3 | 11.3 | 2.1 |
| 11 | $\mathrm{PBu}^{\mathrm{i}}{ }_{3}$ | 143 | 5.7 | 0 | 9.7 |  |  |  |
| 12 | $\mathrm{P}\left(p-\mathrm{MeOC}_{6} \mathrm{H}_{4}\right)_{3}$ | 145 | 10.5 | 2.7 | 14.6 |  |  |  |
| 13 | $\mathrm{P}\left(p-\mathrm{MeC}_{6} \mathrm{H}_{4}\right)_{3}$ | 145 | $11.5{ }^{f}$ | 2.7 | 15.6 |  |  |  |
| 14 | $\mathrm{PPh}_{3}$ | 145 | 13.25 | 2.7 | 17.3 |  |  |  |
| 15 | $\mathrm{P}\left(p-\mathrm{FC}_{6} \mathrm{H}_{4}\right)_{3}$ | 145 | 15.7 | 2.7 | 19.8 |  |  |  |
| 16 | $\mathrm{P}\left(p-\mathrm{ClC}_{6} \mathrm{H}_{4}\right)_{3}$ | 145 | 16.8 | 2.7 | 20.9 |  |  |  |
| 17 | $\mathrm{P}\left(p-\mathrm{F}_{3} \mathrm{CC}_{6} \mathrm{H}_{4}\right)_{3}$ | 145 | $20.5{ }^{\text {e }}$ | 2.7 | 24.6 |  |  |  |
| 18 | $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ | 145 |  | 0 |  | 3.8 | 0.4 | 0 |
| 19 | $\mathrm{PPh}_{2} \mathrm{Pr}^{\mathrm{i}}$ | 150 | 10.9 | 2 |  | 13.8 | 9.6 | 1.5 |
| 20 | $\mathrm{PPh}_{2} \mathrm{Cy}$ | 153 | $9.3{ }^{\text {g }}$ | 2 |  | 13.4 | 9.1 | 1.6 |
| 21 | $\mathrm{PPhPr}^{\mathrm{i}}{ }_{2}$ | 155 | 7.5 | 1 |  | 11.5 | 7.1 | 1.7 |
| 22 | $\mathrm{PPr}^{\mathrm{i}}$ | 160 | 3.45 | 0 | 7.9 |  |  |  |
| 23 | $\mathrm{PPhCy}_{2}$ | 161 | $5.35{ }^{\text {g }}$ | 1 |  | 10.2 | 5.7 | 1.6 |
| 24 | $\mathrm{PCy}_{3}$ | 170 | 1.4 | 0 | 6.2 |  |  |  |

${ }^{a}$ Data are taken from ref. 46. ${ }^{b}$ Data are taken from ref. 20. ${ }^{c}$ Data are taken from ref. 23. ${ }^{d}$ Calculated via eqn. (15). ${ }^{e}$ Data were calculated as described in this paper. ${ }^{f}$ Data are taken from ref. 47. ${ }^{g}$ Estimated based on additivity.


Fig. 6 Plots of $\Delta H^{\circ}$ and $\Delta S^{\circ}$ versus $z_{3}$ for the family of ligands $\mathrm{P}\left(p-\mathrm{MeC}_{6} \mathrm{H}_{4}\right)_{3}, \mathrm{PPh}_{2} \mathrm{Cy}, \mathrm{PPhEt}_{2}, \mathrm{PPhBu}_{2}, \mathrm{PBu}_{3}{ }_{3}$, and $\mathrm{PEt}_{3}$. The $r^{2}$ values are 0.996 and 0.991 for the two plots, respectively.
operative (as shown by the separation of lines in Fig. 9A) and since the datum for $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ lies on the $\mathrm{PR}_{3}$ line, it follows that $E_{\text {ar }}=0$ for $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$.

Since $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ is isosteric to $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ but has $E_{\text {ar }}=0$, its datum will fall along the line determined by $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ only if the aryl effect is not operative. Even when steric effects are operative this is true. The analysis of the heats of reaction for the formation of $\eta-\mathrm{Cp}^{*} \mathrm{RuL}_{2} \mathrm{Cl}$ from $\eta-\mathrm{Cp}^{*} \mathrm{Ru}-$ (cod) $\mathrm{Cl}^{55}$ is an example of this case (Fig. 9B). (The datum for


Fig. 7 A plot of $\chi$ values for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ reported by Bartik ${ }^{20}$ and the $\chi_{z}$ values reported in this paper.


Fig. 8 A plot of $\Delta H^{\circ}$ versus $\chi$ values. The $\chi$ values for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$ were calculated as described in this paper.
$\mathrm{PPh}_{3}$ appears to be an outlier.) (Note that absence of the aryl effect is indicated by a crossing of $\mathrm{PR}_{3}$ and $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ lines at $\chi=4.8{ }^{23}$ ).

Finally, if both steric effects and the aryl effect are operative then the datum for $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ will not fall along the lines determined by either the $\mathrm{PR}_{3}$ or $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ families of ligands. The point, however, will fall along the line that would


Fig. 9 Plots of physicochemical data for $\mathrm{P}_{\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3} \text { and } \mathrm{PR}_{3}(\square) \text {, and }}$ $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}(\mathrm{O})$ versus the electronic parameter $\chi$. (A) Since there is no significant steric effect in $\Delta H^{\circ}$ for the reduction of $\eta-\mathrm{Cp}(\mathrm{CO})$ $(\mathrm{L}) \mathrm{Fe}(\mathrm{COMe})^{+}$and since $E_{\text {ar }}=0$ for $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$, the datum for $\mathrm{P}\left(\mathrm{NC}_{4}{ }^{-}\right.$ $\left.\mathrm{H}_{8}\right)_{3}$ lies along the line defined by $\mathrm{PR}_{3}$. (B) Since there is no significant 'aryl effect' in $-\Delta H_{\mathrm{rx}}$ for the transformation of $\eta-\mathrm{Cp} * \mathrm{Ru}(\operatorname{cod}) \mathrm{Cl}$ into $\eta-\mathrm{Cp} * \mathrm{RuL} \mathbf{L}_{2} \mathrm{Cl}$ and since $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ is isosteric with $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$, the datum for $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ lies along the line defined by $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$. (The point for $\mathrm{PPh}_{3}$ appears to be an outlier.) (C) The average $\mathrm{Ru}-\mathrm{P}$ bond length for $\eta-\mathrm{Cp}^{*} \mathrm{RuL}_{2} \mathrm{Cl}$ depends on both steric effects and the 'aryl effect', hence, the datum for $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$ is not on either line. The point is, however, on the hypothetical (dashed) line that would be determined by $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ if there were no aryl effect. (The dashed line intersects the $\mathrm{PR}_{3}$ line at $\chi=4.8$.)
have been determined by $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ if there were no aryl effect. The analysis of the average $\mathrm{Ru}-\mathrm{P}$ bond lengths in $\eta$ $\mathrm{Cp}^{*} \mathrm{RuL}_{2} \mathrm{Cl}^{55,56}$ illustrates this case (Fig. 9C). Based on these results, we believe that $\chi=0.4$ is a reasonable value for $\mathrm{P}\left(\mathrm{NC}_{4}-\right.$ $\left.\mathrm{H}_{8}\right)_{3}$ and that this ligand behaves more like a trialkylphosphine.

## Conclusions

It had been previously suggested that the observation of isoequilibrium (or isokinetic) behavior indicated that the free energy of a process was responding to a single stereoelectronic parameter. Herein, we have shown rigorously for a three parameter model that the general case is that isoequilibrium behavior is observed when $\Delta G^{\circ}$ responds to a linear combin-
ation of two of the parameters. We call this combination $z_{3}$. Furthermore, these two parameters do not have to be related. $\Delta H^{\circ}$ and $\Delta S^{\circ}$ also respond linearly to $z_{3}$ for a family of ligands. We showed how to use the linear relationship between $\Delta H^{\circ}$ and $z_{3}$ to calculate values of $\chi$ and $E_{\text {ar }}$ for $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$. With one exception, the values of $\chi$ that we obtained do not differ greatly from the values obtained by Bartik via analysis of the $v_{\text {co }}$ values of $\mathrm{Ni}(\mathrm{CO})_{3} \mathrm{~L}$. The $E_{\text {ar }}$ values appear to be sensitive to the nature of R in $\mathrm{PPh}_{i} \mathrm{R}_{3-i}$. For $\mathrm{R}=$ isopropyl and cyclohexyl, $E_{\text {ar }}$ values deviate significantly from the previously assigned values of 1 and 2. Thus, we have used isoequilibrium behavior to determine the stereoelectronic parameters of ligands relative to a standard set of $\mathrm{PR}_{3}$ and $\mathrm{P}\left(p-\mathrm{XC}_{6} \mathrm{H}_{4}\right)_{3}$ ligands. Using this methodology, we calculated $\chi=0.4 \pm 1.0$ and $E_{\text {ar }}=0$ for $\mathrm{P}\left(\mathrm{NC}_{4} \mathrm{H}_{8}\right)_{3}$, values that had not been reported previously.

## Experimental

## General procedures

All manipulations and preparations were carried out under argon using standard techniques. Acetonitrile (J. T. Baker HPLC grade), which was purified by distillation from $\mathrm{P}_{2} \mathrm{O}_{5}$, was then kept refluxing over $\mathrm{CaH}_{2}$ and distilled immediately prior to use. Tetrabutylammonium hexafluorophosphate (TBAH) (Aldrich) was recrystallized from warm ethyl acetate; before use it was heated in vacuo to remove residual solvent. The phosphines (Aldrich, Lancaster and Strem) were used as received. The $\eta-\mathrm{Cp}(\mathrm{CO})(\mathrm{L}) \mathrm{Fe}(\mathrm{COMe})$ complexes were synthesized according to literature methods. ${ }^{57}$
The $E^{\circ}$ values for the $\eta-\mathrm{Cp}(\mathrm{CO})(\mathrm{L}) \mathrm{Fe}(\mathrm{COMe})^{+/ 0}$ couple were obtained via cyclic voltammetry, and were measured relative to acetylferrocene. Since there was no significant decomposition of the electrochemically generated species, the $E^{\circ}$ values could be obtained by averaging the voltage of the peak potentials of the cyclic voltammogram. Each measurement was taken between 5 and 10 times. The measurements were then repeated with a fresh sample and found to agreed with the original measurements. This leads to an error of $\pm 0.0007 \mathrm{~V}$ in the $E^{\circ}$ values.

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